

# Supporting Information

## Anisotropically Enhanced Second Harmonic Generation in a WS<sub>2</sub> Nanoparticle Driven by Optical Resonances

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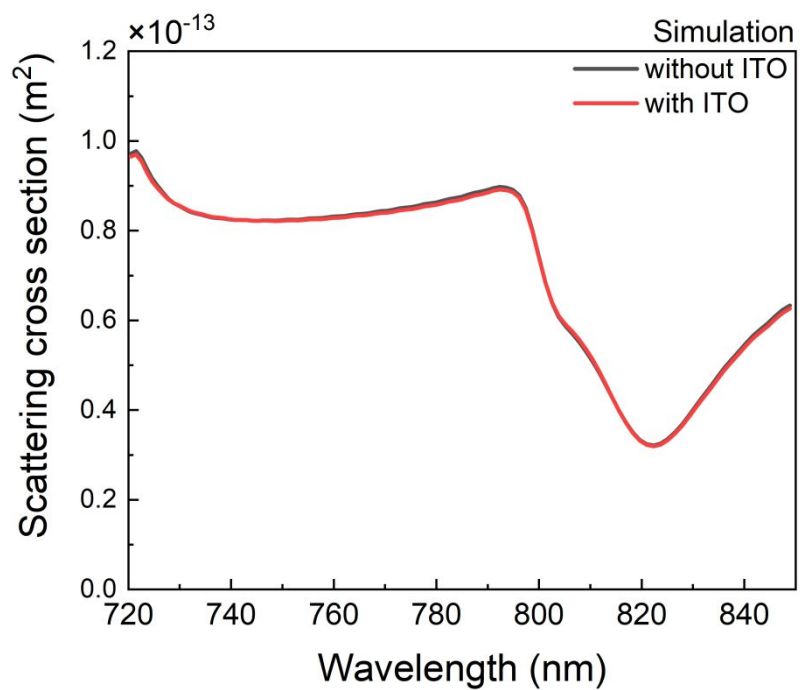
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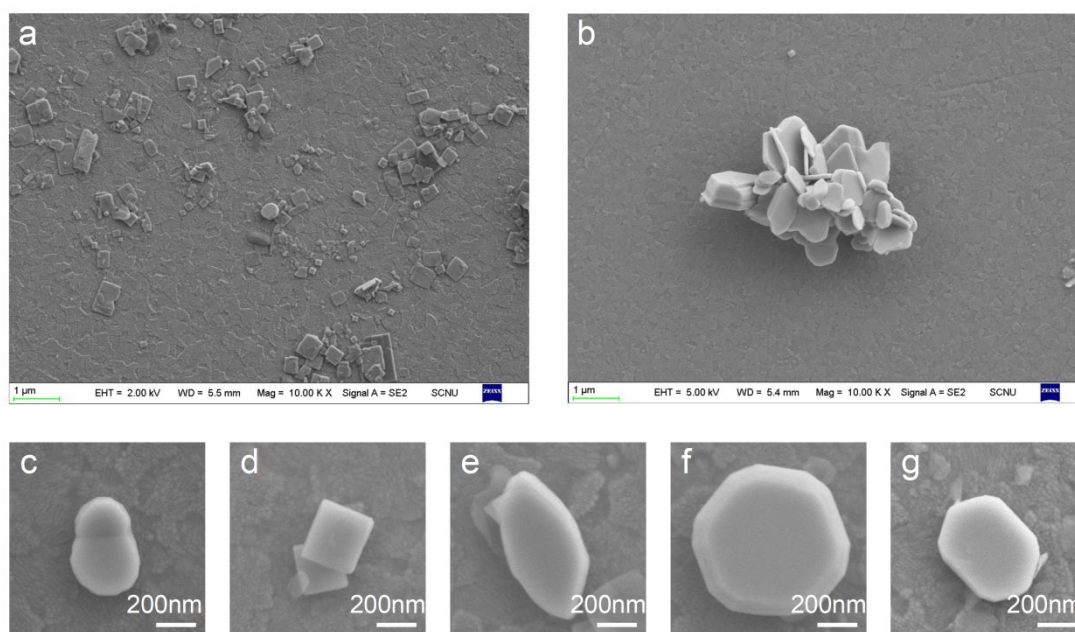
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1. Simulated scattering spectra for a WS<sub>2</sub> nanoparticle placed on a silica (SiO<sub>2</sub>) substrate without and with a thin ITO film.



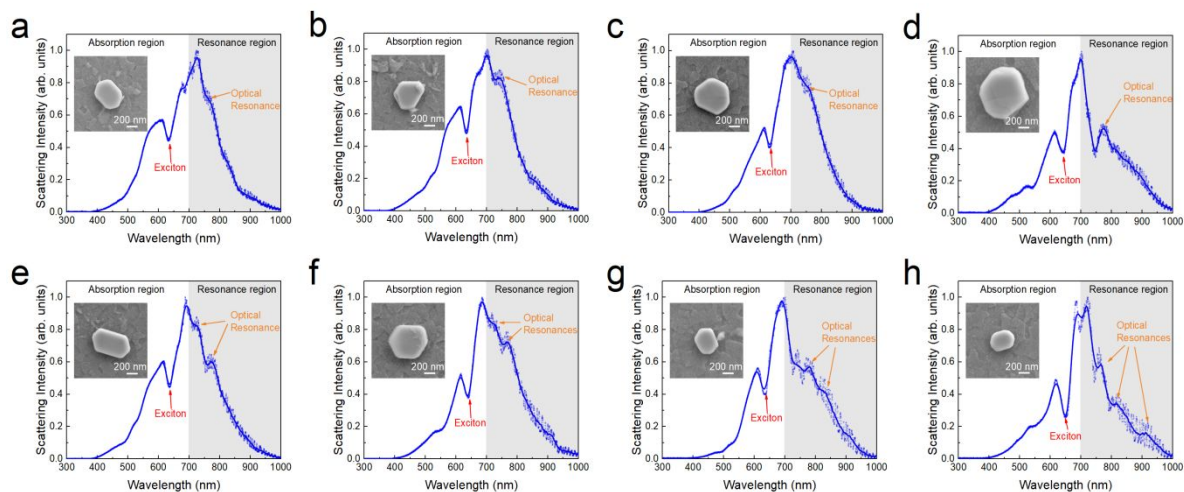
**Figure S1.** Simulated scattering spectra of a WS<sub>2</sub> nanoparticle placed on a silica (SiO<sub>2</sub>) substrate without (black curve) and with (red curve) a thin ITO film of 10 nm.

## 2. Morphology characterization of WS<sub>2</sub> nanoparticles.



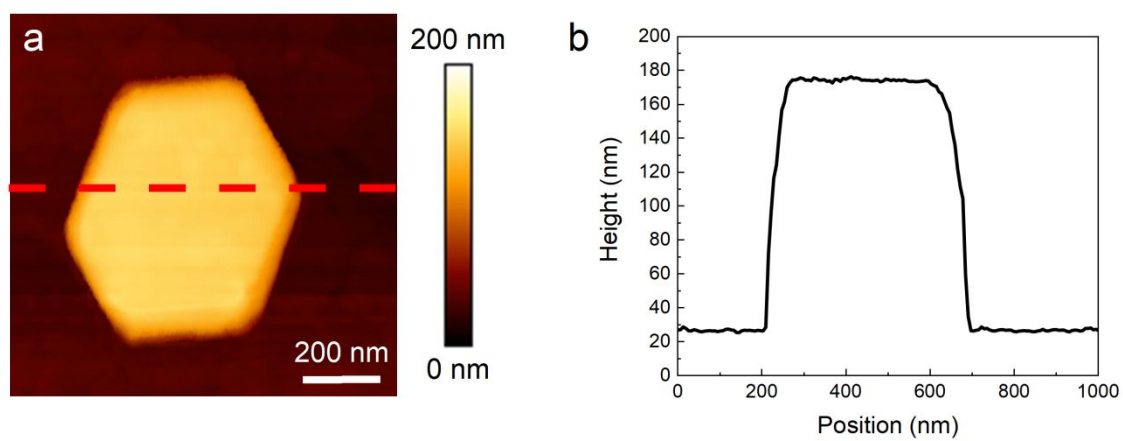
**Figure S2.** (a-b) SEM images of WS<sub>2</sub> nanoparticles distributed on an ITO/SiO<sub>2</sub> substrate. (c-g) SEM images of single WS<sub>2</sub> nanoparticles with different shapes.

### 3. SEM images and scattering spectra of more WS<sub>2</sub> nanoparticles



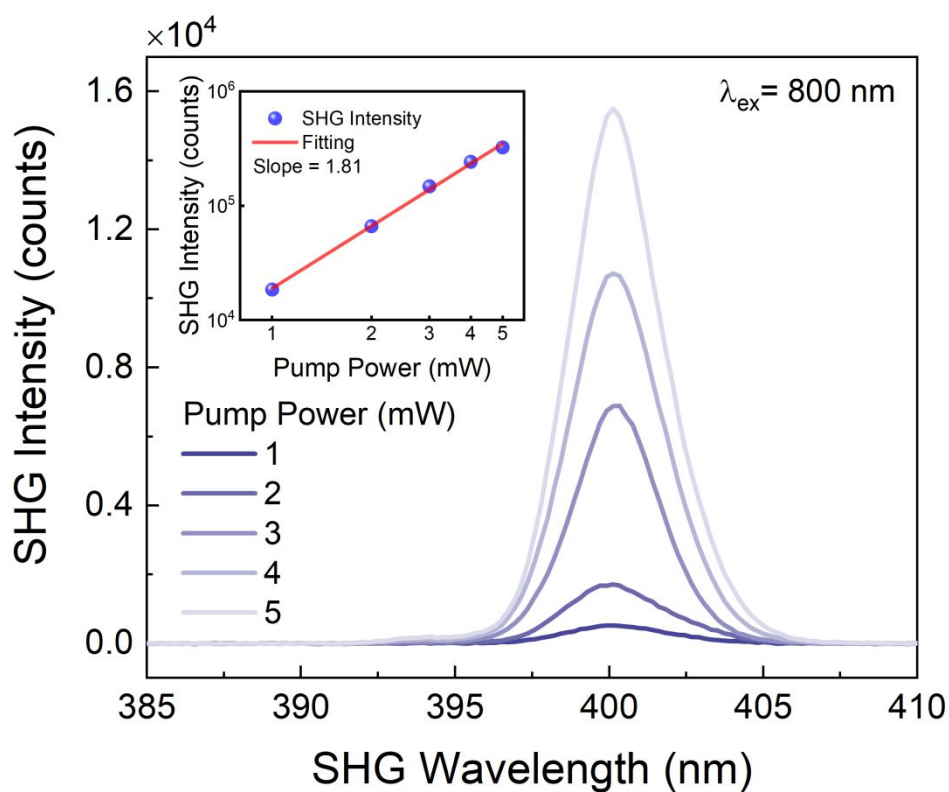
**Figure S3.** (a-h) Scattering spectrum of more WS<sub>2</sub> nanoparticles. The SEM images of the WS<sub>2</sub> nanoparticles are shown in the insets.

#### 4. Height characterization of WS<sub>2</sub> nanoparticles



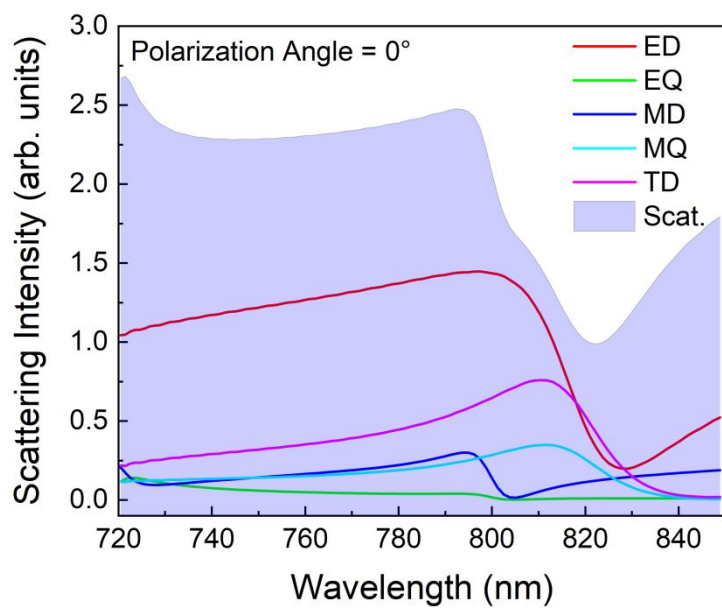
**Figure S4.** (a) AFM images of the WS<sub>2</sub> nanoparticle shown in Figure 2a. (b) Height profile along the dashed line in (a).

## 5. Dependence of the SHG intensity of a WS<sub>2</sub> nanoparticle on the pumping power



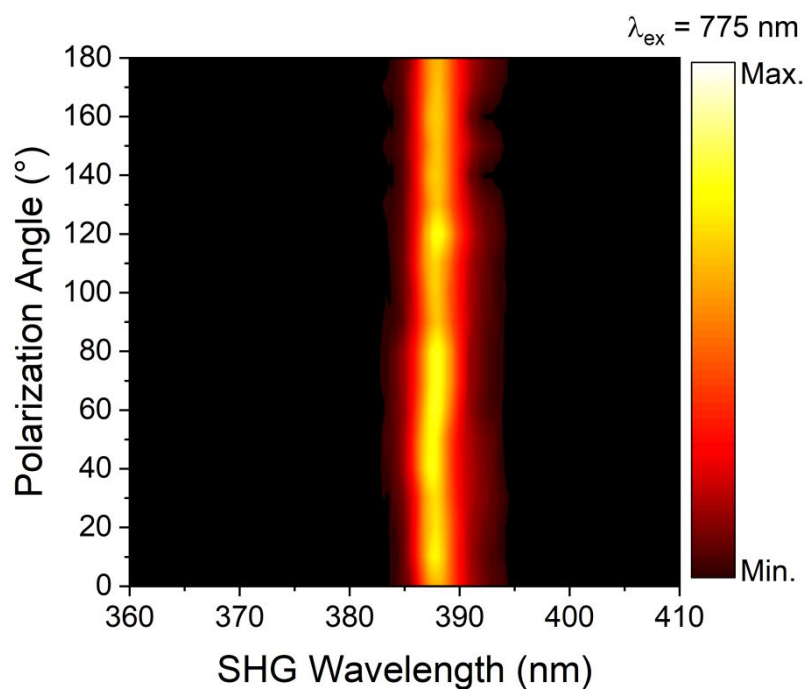
**Figure S5.** SHG spectra measured for a WS<sub>2</sub> nanoparticle by using femtosecond laser light ( $\lambda_{\text{ex}} = 800 \text{ nm}$ ) with different pumping powers. The dependence of the SHG intensity on the pumping power is shown in the inset.

## 6. Multipolar decomposition of the scattering spectrum of a WS<sub>2</sub> nanoparticle



**Figure S6.** Scattering spectrum simulated for the WS<sub>2</sub> nanoparticle shown in Figure 2 and its decomposition into the Mie resonances. The contribution of TD is included in the decomposition of the scattering spectrum.

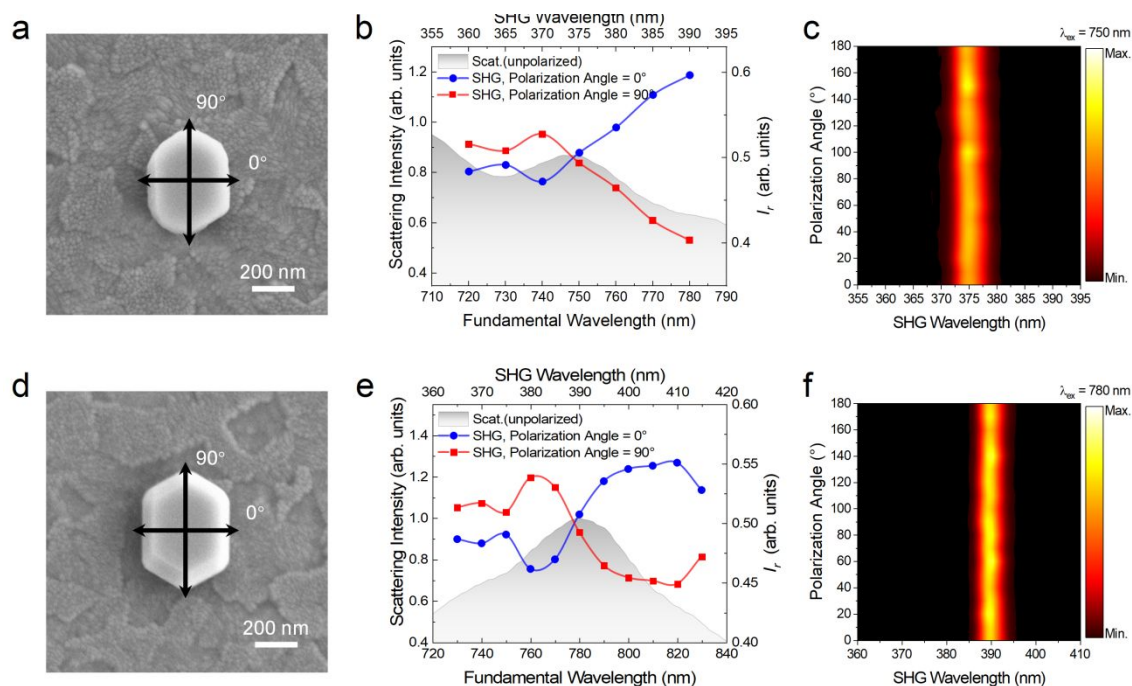
7. Dependence of SHG intensity of a WS<sub>2</sub> nanoparticle on the polarization angle of the excitation laser light ( $\lambda_{\text{ex}} = 775 \text{ nm}$ )



**Figure S7:** Dependence of the SHG intensity on the polarization angle of the excitation laser light ( $\lambda_{\text{ex}} = 775 \text{ nm}$ ) measured for a WS<sub>2</sub> nanoparticle.

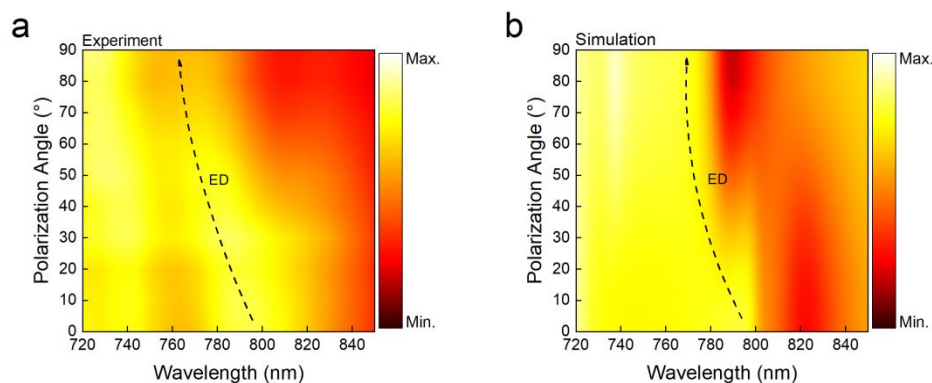


## 8. Polarization-dependent SHG intensity observed in more WS<sub>2</sub> nanoparticles

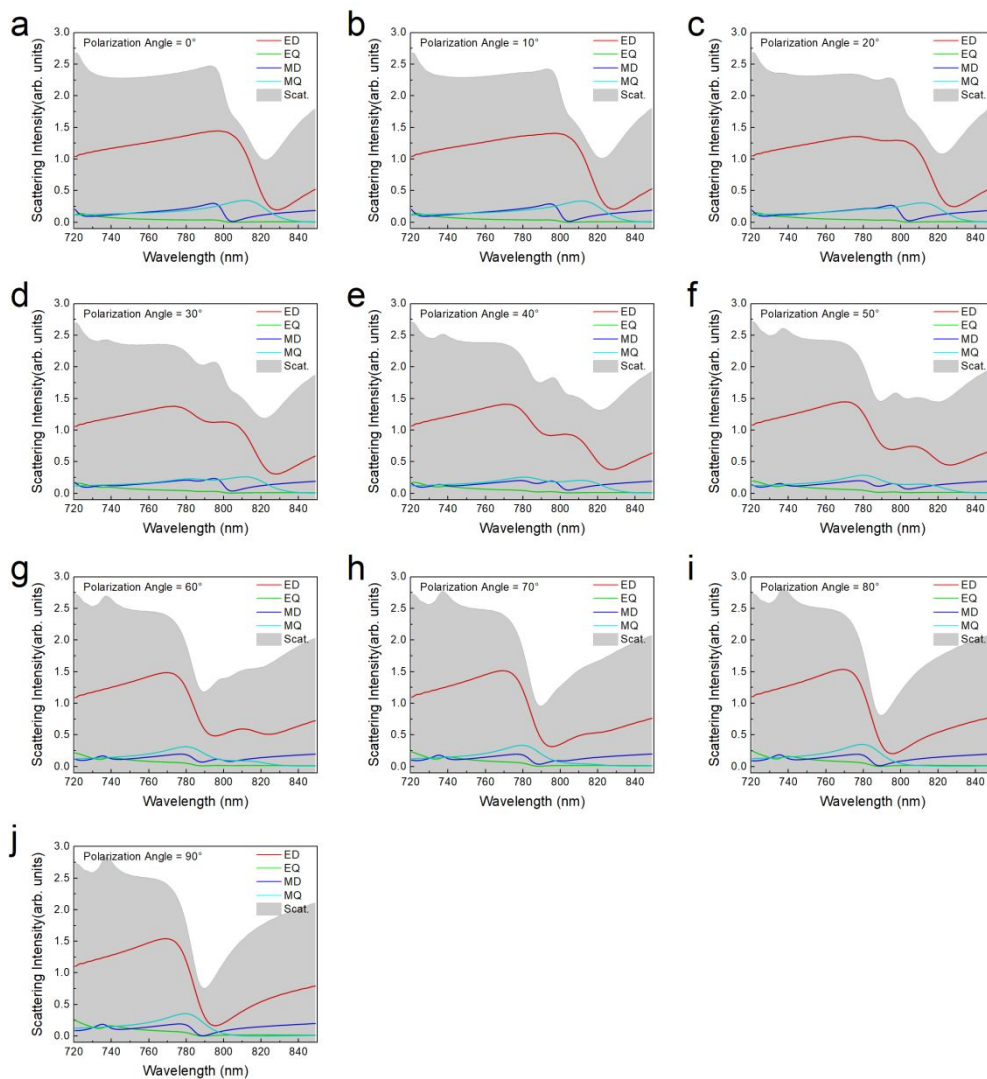


**Figure S8.** (a), (d) SEM images of another two hexagonal-prism-like WS<sub>2</sub> nanoparticles. (b), (e) Dependence of the relative SHG intensity on the excitation wavelength calculated for the WS<sub>2</sub> nanoparticles at polarization angles of  $\theta = 0^\circ$  and  $\theta = 90^\circ$ . In each case, the scattering spectrum of the WS<sub>2</sub> nanoparticle illuminated with unpolarized white light is provided for reference. (c), (f) Dependence of SHG intensity on the polarization angle of the excitation light observed at the scattering peak. (b) and (c) correspond to (a), (e) and (f) correspond to (d).

**9. Evolution of the scattering spectrum with increasing polarization angle and multipole decomposition of the scattering spectrum for a hexagonal-prisms-like WS<sub>2</sub> nanoparticle.**

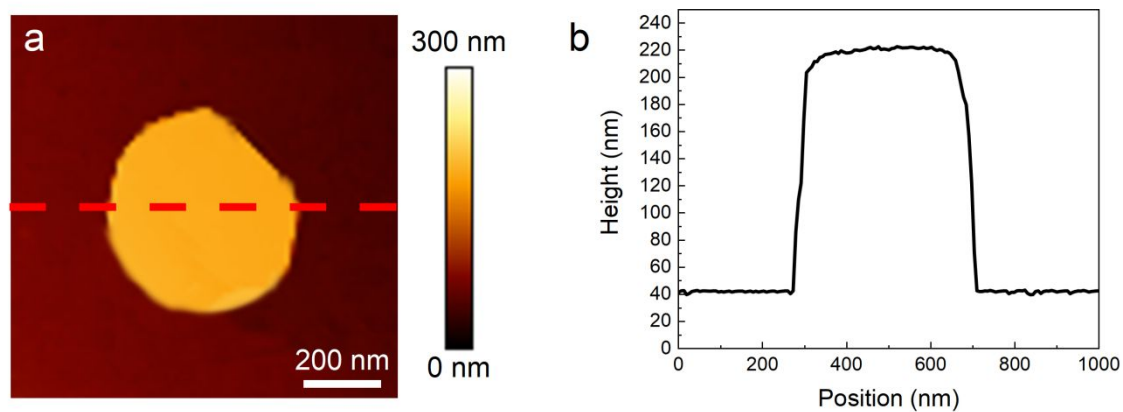


**Figure S9.** (a-b) Evolution of the scattering spectrum with increasing polarization angle observed for a hexagonal-prisms-like WS<sub>2</sub> nanoparticle. (a) experiment; (b) simulation.



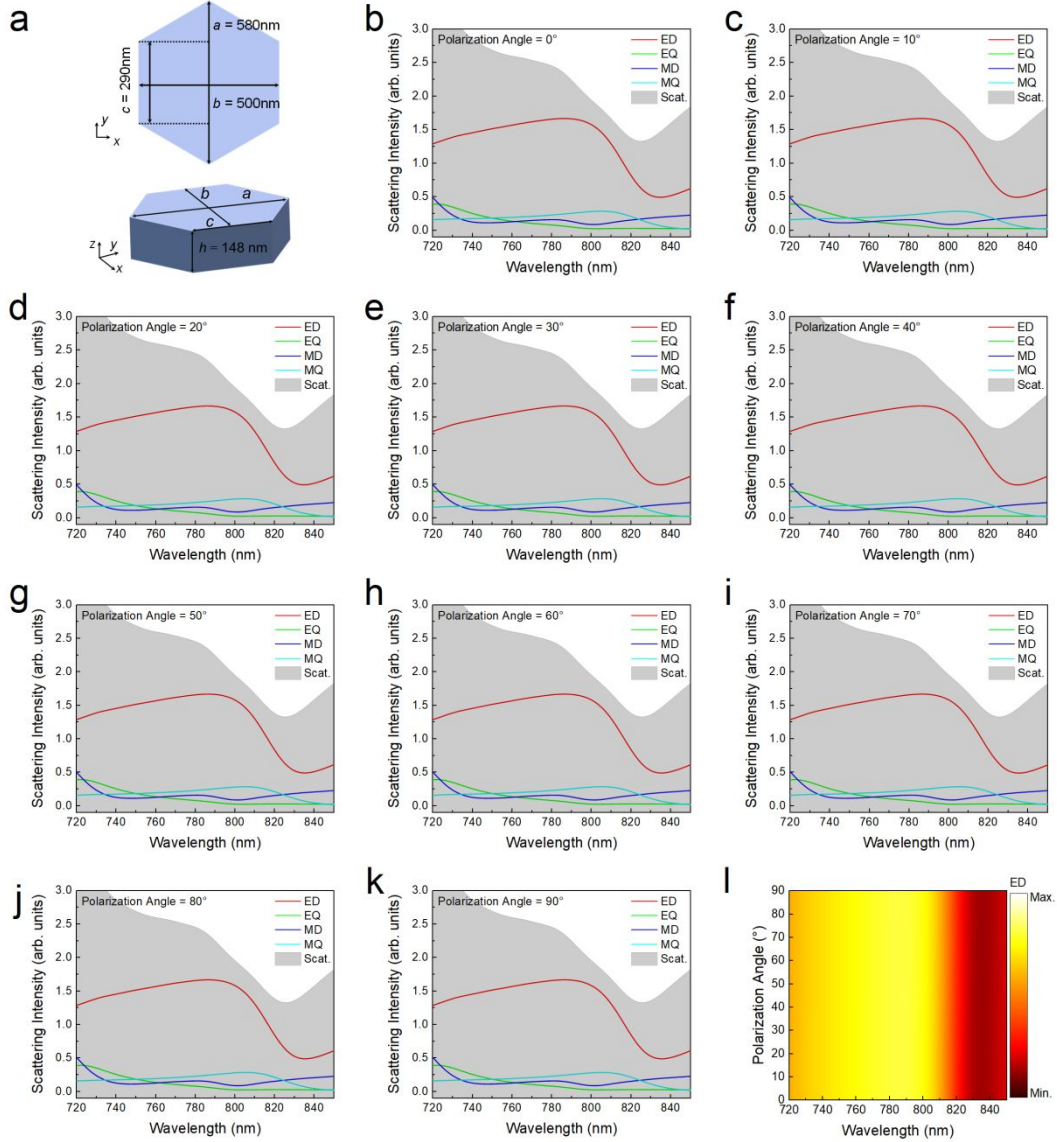
**Figure S10.** (a-j) Scattering spectra simulated for a hexagonal-prisms-like WS<sub>2</sub> nanoparticle ( $a = 580$  nm,  $b = 444$  nm,  $c = 312$  nm,  $h = 148$  nm) at different polarization angles ranging from  $\theta = 0^\circ$  to  $\theta = 90^\circ$ . In each case, the scattering spectrum is decomposed into the contributions of Mie resonances.

## 10. Height characterization of WS<sub>2</sub> nanoparticles



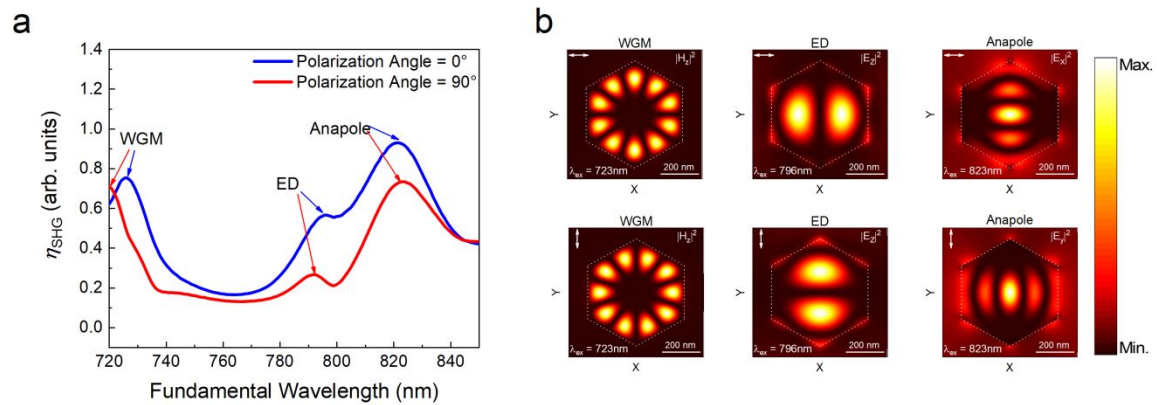
**Figure S11.** (a) AFM images of the WS<sub>2</sub> nanoparticle shown in Figure 4a. (b) Height profile along the dashed line in (a).

## 11. Polarization-dependent scattering spectra simulated for a hexagonal-prism $\text{WS}_2$ nanoparticle



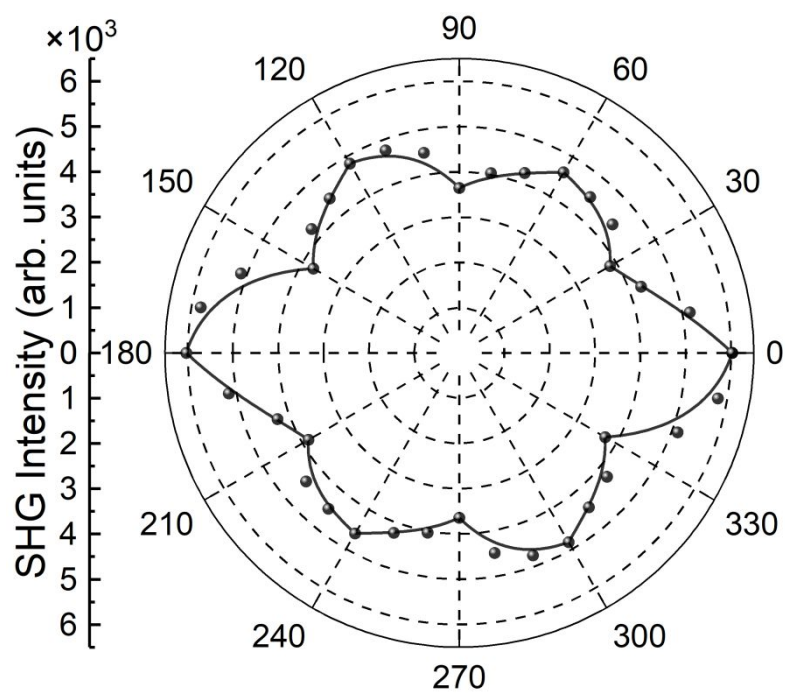
**Figure S12.** (a) Structure of a hexagonal-prism  $\text{WS}_2$  nanoparticle. (b-k) Scattering spectra simulated for the hexagonal-prism  $\text{WS}_2$  nanoparticle ( $a = 580\text{ nm}$ ,  $b = 500\text{ nm}$ ,  $c = 290\text{ nm}$ ,  $h = 148\text{ nm}$ ) at polarization angles ranging from  $\theta = 0^\circ$  to  $\theta = 90^\circ$ . In each case, the scattering spectrum is decomposed into the contributions of Mie resonances of different orders. (l) Evolution of the ED resonance with increasing polarization angle simulated for the hexagonal-prism  $\text{WS}_2$  nanoparticle.

## 12. Electric and magnetic field distributions calculated at the optical resonances supported by a hexagonal-prism $\text{WS}_2$ nanoparticle



**Figure S13.** (a) Dependence of the SHG efficiency on the excitation wavelength simulated for the hexagonal-prism  $\text{WS}_2$  nanoparticle ( $a = 580$  nm,  $b = 500$  nm,  $c = 290$  nm,  $h = 148$  nm) at polarization angles of  $\theta = 0^\circ$  and  $\theta = 90^\circ$ . (b) Electric/magnetic field distributions calculated at different optical resonances. In each case, the polarization of the excitation light is indicated by an arrow.

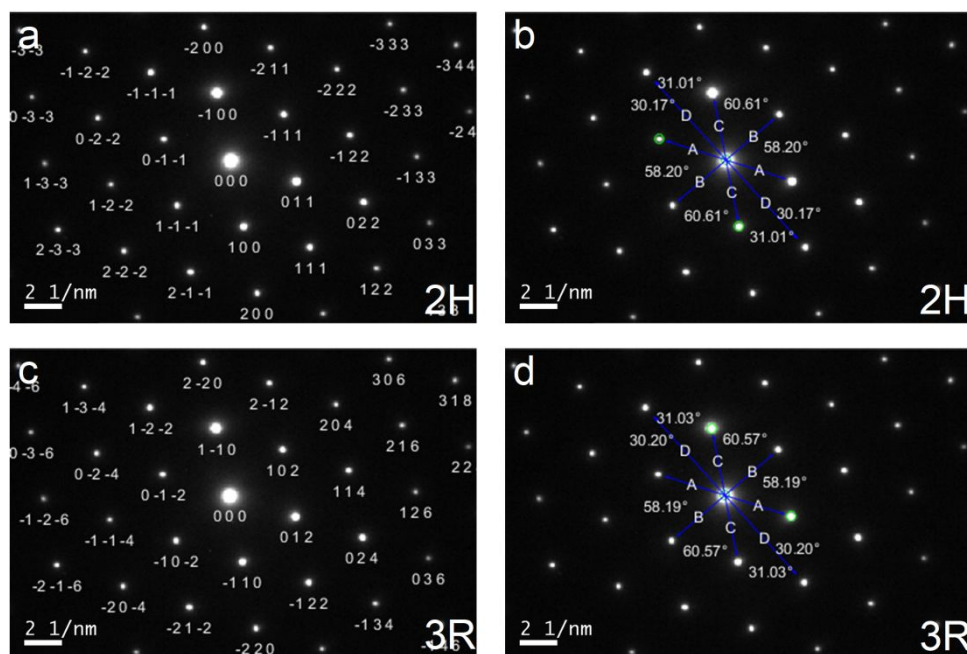
**13. Dependence of the SHG intensity on the polarization angle observed for a WS<sub>2</sub> monolayer**



**Figure S14.** SHG intensities measured for a WS<sub>2</sub> monolayer at different polarization angles.



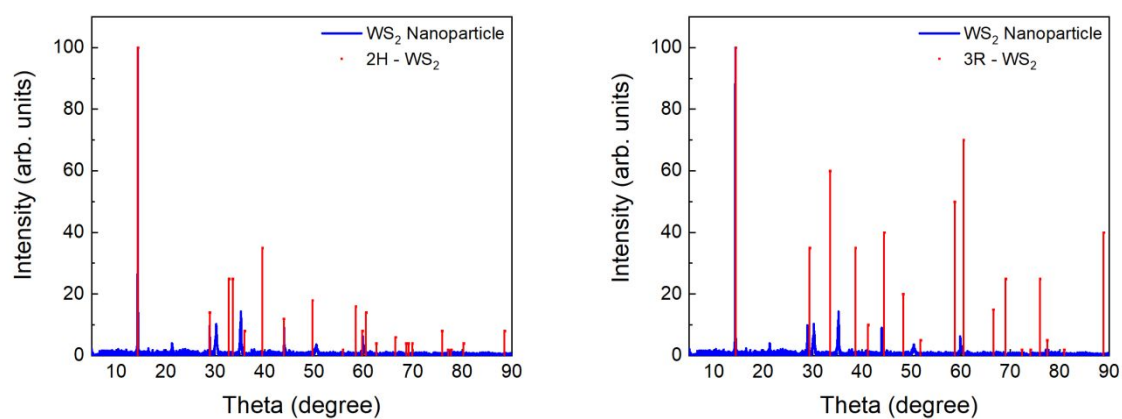
## 14. Analysis of the crystal structure of WS<sub>2</sub>



**Figure S15:** Comparison of the electron diffraction pattern with 2H (a,b) and 3R (c,d).

**Table S1:** Parameters extracted from the electron diffraction of the WS<sub>2</sub> nanoparticle

polymorph	2H	3R
<b>d spacing</b>	A: 0.277 B: 0.276 C: 0.285 D: 0.163	A: 0.278 B: 0.276 C: 0.285 D: 0.163
<b>Total angular dist.</b>	0.52	1.82
<b>d-spacing STDEV</b>	0.0014	0.0022



**Figure S16.** Comparison of the X-ray diffraction spectrum measured for the WS<sub>2</sub> nanoparticle with those of 2H and 3R phases.